

Lesson 6: Solve for Unknown Angles—Angles and Lines at a Point

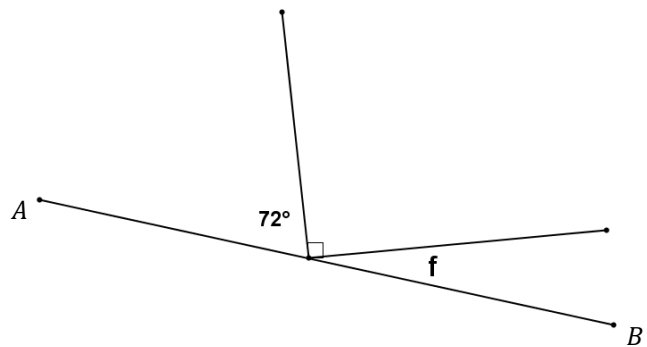
Classwork

Discussion

Two angles $\angle AOC$ and $\angle COB$, with a common side \overrightarrow{OC} , are _____ if C belongs to the interior of $\angle AOB$. The sum of angles on a straight line is 180° . Two angles are called supplementary if the sum of their measures is _____; two angles are called complementary if the sum of their measures is _____. Describing angles as supplementary or complementary refers only to the measures of their angles; the positions of the angles or whether the pair of angles is adjacent to each other is not part of the definition.

In the figure, AB is a straight line.
Find the measure of $\angle f$.

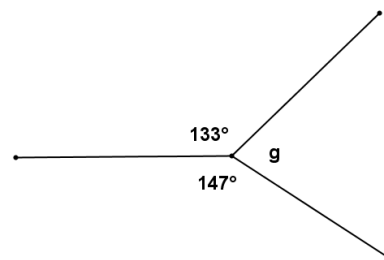
$\angle f =$ _____



The total measure of adjacent angles around a point is _____.

Find the measure of $\angle g$.

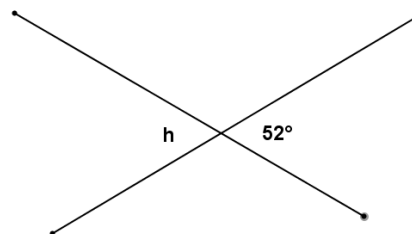
$\angle g =$ _____



Vertical angles have _____ measure.

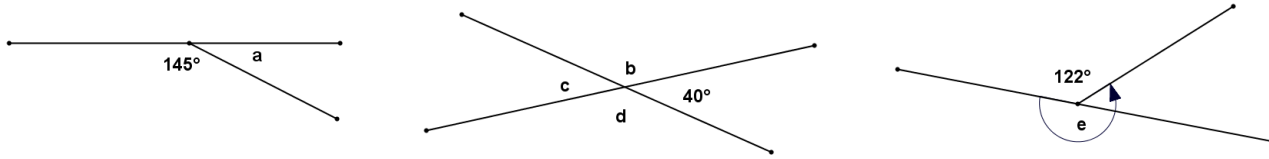
Find the measure of $\angle h$.

$\angle h =$ _____



Example 1

Find the measures of each labeled angle. Give a reason for your solution.

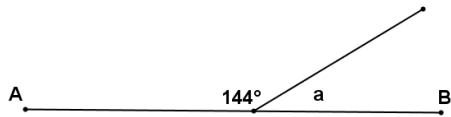


Angle	Angle measure	Reason
$\angle a$		
$\angle b$		
$\angle c$		
$\angle d$		
$\angle e$		

Exercises

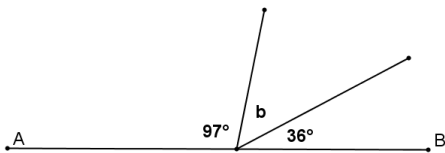
In the figures below, AB , CD , and EF are straight lines. Find the measure of each marked angle or find the unknown numbers labeled by the variables in the diagrams. **Give reasons** for your calculations. Show all the steps to your solution.

1.



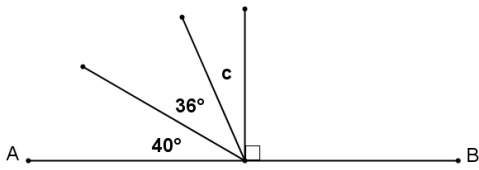
$\angle a =$ _____

2.



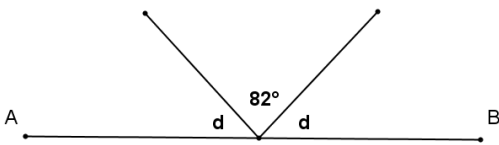
$\angle b =$ _____

3.



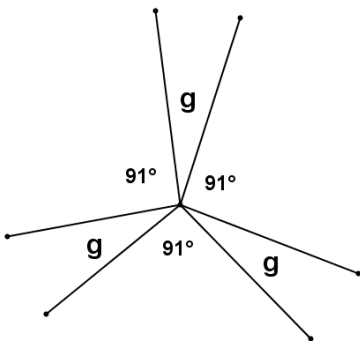
$\angle c =$ _____

4.



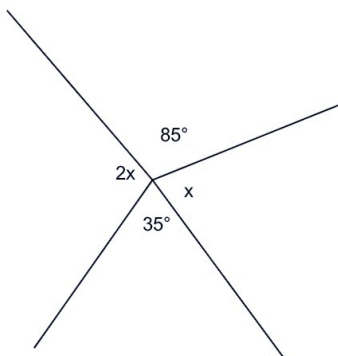
$\angle d =$ _____

5.



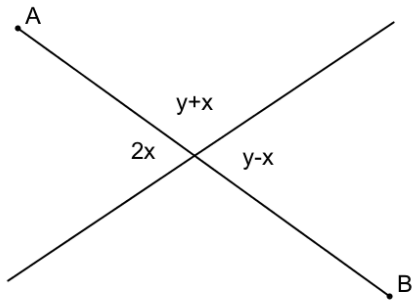
$\angle g =$ _____

6.



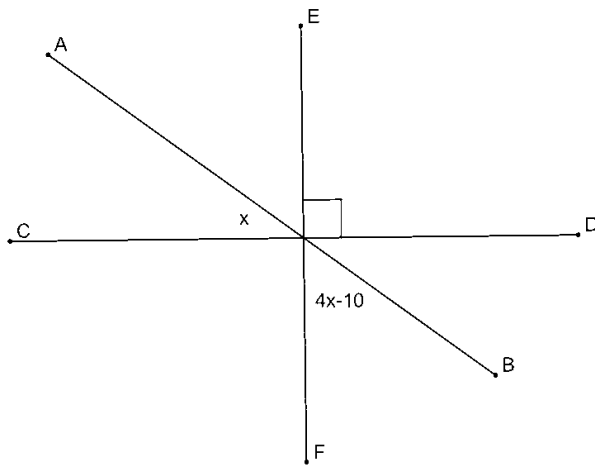
$x =$ _____

7.



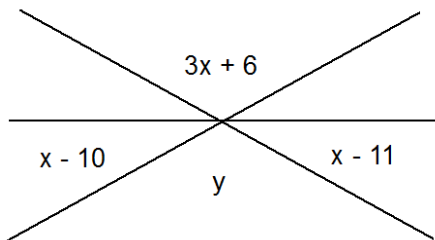
$y = \underline{\hspace{2cm}}$ $x = \underline{\hspace{2cm}}$

8.



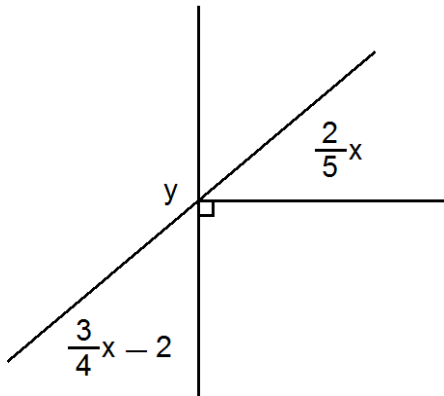
$x = \underline{\hspace{2cm}}$

9.



$x = \underline{\hspace{2cm}}$

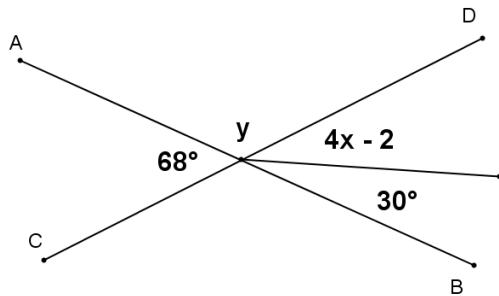
10.



$x = \underline{\hspace{2cm}}$ $y = \underline{\hspace{2cm}}$

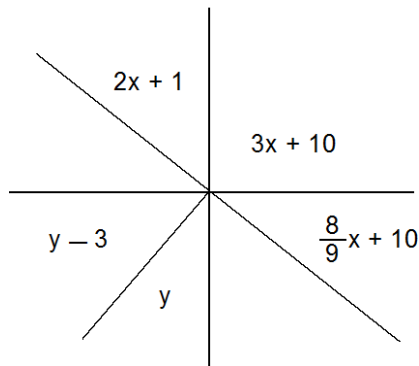
For Problems 11–12, find the values of x and y . Show all the steps to your solution.

11.



$x = \underline{\hspace{3cm}}$

12.



$x = \underline{\hspace{2cm}}$ $y = \underline{\hspace{2cm}}$

Relevant Vocabulary

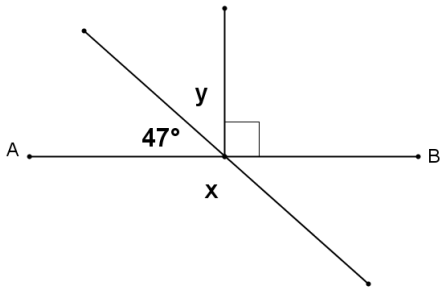
Straight Angle: If two rays with the same vertex are distinct and collinear (i.e., they form a line), then each of the angles formed by the line is called a *straight angle*.

Vertical Angles: Two angles are *vertical angles* (or *vertically opposite angles*) if their sides form two pairs of opposite rays.

Problem Set

Find the value of x and/or y in each diagram below. Show all the steps to your solution.

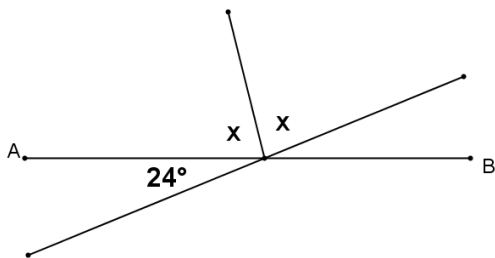
1.



$x =$ _____

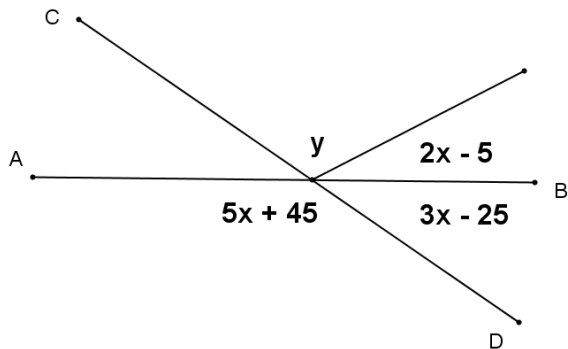
$y =$ _____

2.



$x =$ _____

3.



$x =$ _____

$y =$ _____