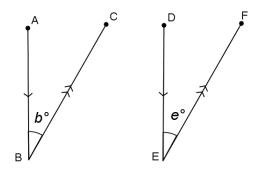


Lesson 10: Unknown Angle Proofs—Proofs with Constructions

Classwork

Opening Exercise

In the figure on the right, $\overline{AB} \mid \mid \overline{DE}$ and $\overline{BC} \mid \mid \overline{EF}$. Prove that b = e (Hint: Extend \overline{BC} and \overline{ED} .)



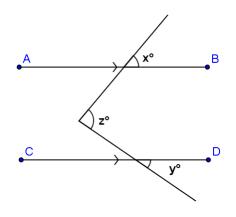
Proof:

In the previous lesson, you used deductive reasoning with labeled diagrams to prove specific conjectures. What is different about the proof above?

Adding or extending segments, lines, or rays (referred to as **auxiliary**) is frequently useful in demonstrating steps in the deductive reasoning process. Once \overline{BC} and \overline{ED} were extended, it was relatively simple to prove the two angles congruent based on our knowledge of alternate interior angles. Sometimes there are several possible extensions or additional lines that would work equally well.

For example, in this diagram, there are at least two possibilities for auxiliary lines. Can you spot them both?

Given: $\overline{AB} \mid \mid \overline{CD}$. Prove: z = x + y.





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Discussion

Here is one possibility:

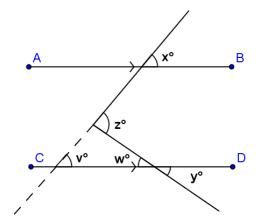
Given: $\overline{AB} \mid \mid \overline{CD}$. Prove: z = x + y.

Extend the transversal as shown by the dotted line in the diagram. Label angles v and w, as shown.

What do you know about v and x?

About angles w and y? How does this help you?

Write a proof using the auxiliary segment drawn in the diagram to the right.



Another possibility appears here:

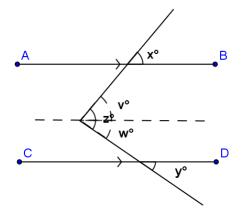
Given: $\overline{AB} \mid \mid \overline{CD}$. Prove: z = x + y.

Draw a segment parallel to \overline{AB} through the vertex of angle z. This divides $\angle z$ into angles v and w, as shown.

What do you know about angles v and x?

About angles w and y? How does this help you?

Write a proof using the auxiliary segment drawn in this diagram. Notice how this proof differs from the one above.





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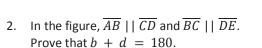
E

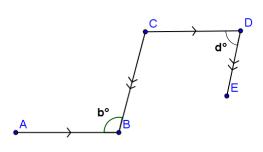
С

Examples

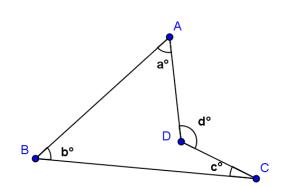
1. In the figure, $\overline{AB} \mid \mid \overline{CD}$ and $\overline{BC} \mid \mid \overline{DE}$. Prove that $\angle ABC = \angle CDE$.

(Where will you draw an auxiliary segment?)





3. In the figure, prove that d = a + b + c.





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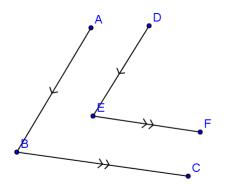


GEOMETRY

M1

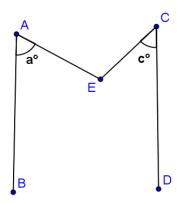
Problem Set

1. In the figure, $\overline{AB} \mid |\overline{DE}$ and $\overline{BC} \mid |\overline{EF}$. Prove that $\angle ABC = \angle DEF$.



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2. In the figure, $\overline{AB} \mid \mid \overline{CD}$. Prove that $\angle AEC = a + c$.





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