



Name \_\_\_\_\_

**Lesson 12a: Digging Deeper into Parallel Lines and Proofs**

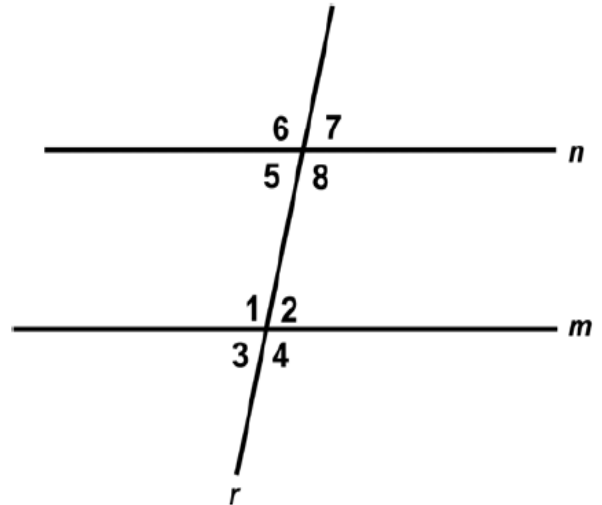
**Warm Up**

**LEARNING TARGET**

**I CAN use geometric facts about parallel lines to prove other geometric facts.**

**Exercise #1:** In the following diagram, lines  $m$  and  $n$  are parallel ( $m \parallel n$ ) and are cut by transversal line  $r$ . Angles have been numbered to make identifying them easier.

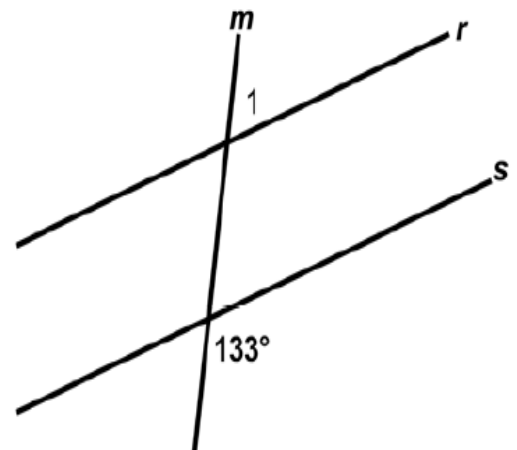
(a) Give all **corresponding angle pairs**. What is true about their measures?



(b) Give all **alternate interior angle pairs**. What is true about their measures?

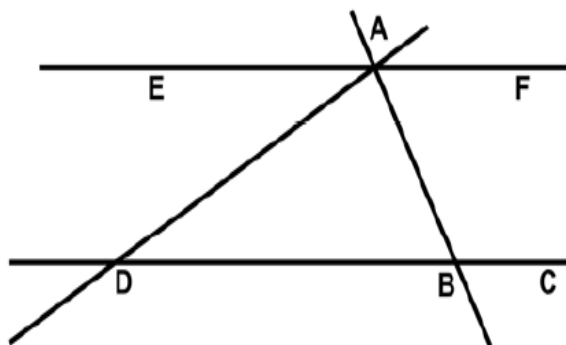
**Mini Lesson**

**Exercise #2:** In the diagram below,  $r \parallel s$  and are cut by transversal  $m$ . Explain why  $m\angle 1 = 47^\circ$ .



**Exercise #3:** In the diagram shown,  $\overline{EF} \parallel \overline{DC}$ ,  $m\angle ABC = 112^\circ$  and  $m\angle EAD = 24^\circ$ . Which of the following represent the measure of  $\angle DAB$ ?

- (1)  $24^\circ$
- (2)  $44^\circ$
- (3)  $88^\circ$
- (4)  $112^\circ$

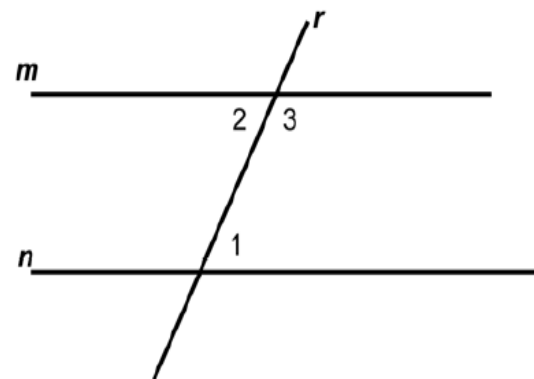


**Exercise #4:** In the following diagram lines  $m$  and  $n$  are parallel and cut by straight line transversal  $r$ . Angles are numbered as shown.

Prove:  $\angle 1$  and  $\angle 3$  are supplementary

Make a plan:

SHOW:

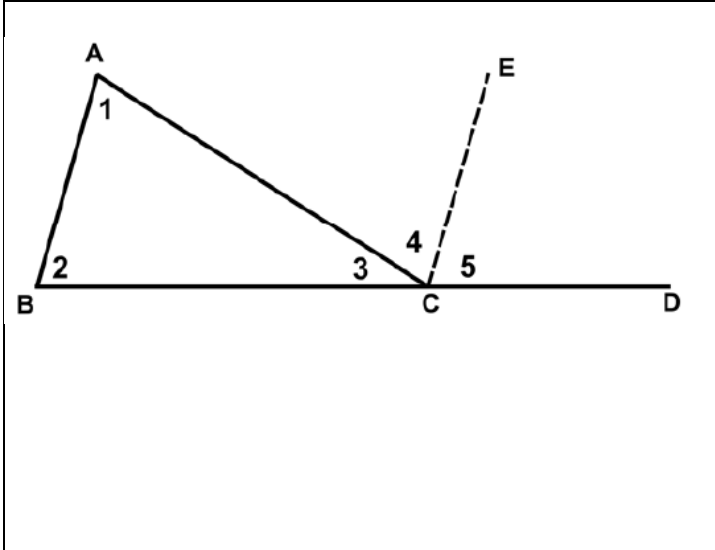


STATEMENT

REASON

**Exercise #5:** In the following diagram,  $\triangle ABC$  has been drawn and side  $\overline{BC}$  has been extended to point  $D$ . Point  $E$  has been located such that **auxiliary** segment  $\overline{CE}$  is parallel to  $\overline{AB}$ .

Given that  $\overline{AB} \parallel \overline{CE}$ :



- a. What angle must be equal in measure to  $\angle 1$ ? Why?
  
- b. What angle must be equal in measure to  $\angle 2$ ? Why?

**Prove:**  $m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ$

**SHOW:**

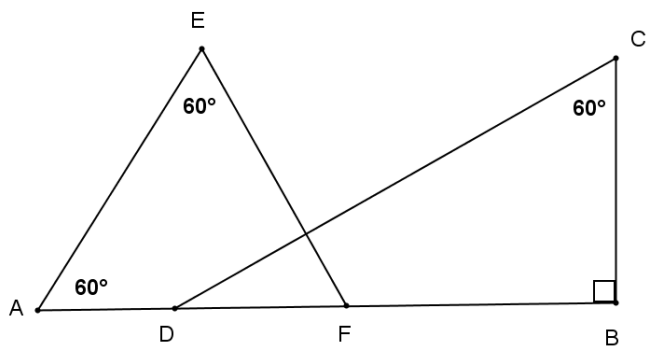
Make a plan:

STATEMENT	REASON

**Work Time**

1. Given the diagram below:

Prove:  $\overline{DC} \perp \overline{EF}$ .



Make a plan that can be used to write the proof:

(What geometric facts are relevant?)

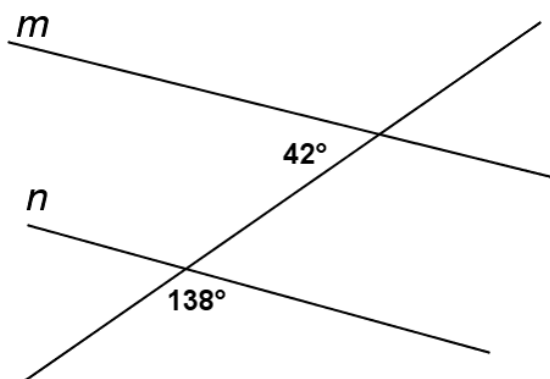
SHOW:

Write out your proof:

STATEMENT	REASON

2. In the diagram below, prove that  $m \parallel n$ . Make a plan:

**SHOW:**

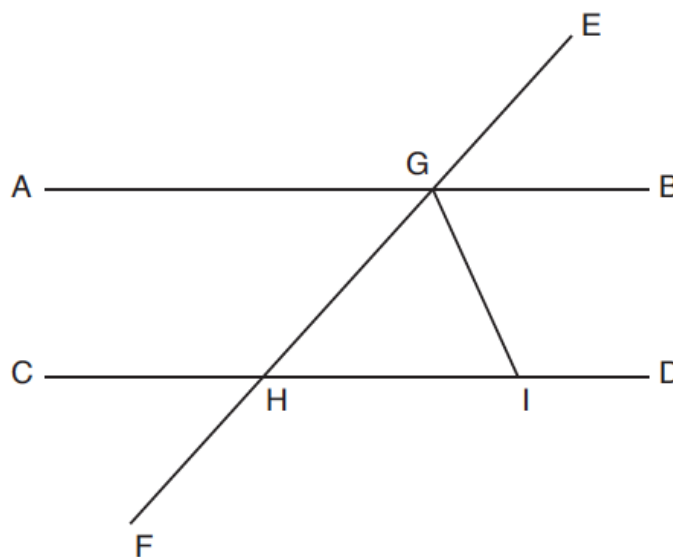


Write out your proof:

STATEMENT	REASON

(from the June 2017 Geometry Regents)

32 In the diagram below,  $\overline{EF}$  intersects  $\overline{AB}$  and  $\overline{CD}$  at  $G$  and  $H$ , respectively, and  $\overline{GI}$  is drawn such that  $\overline{GH} \cong \overline{IH}$ .



If  $m\angle EGB = 50^\circ$  and  $m\angle DIG = 115^\circ$ , explain why  $\overline{AB} \parallel \overline{CD}$ .