

Lesson #3: Recursive Formulas

Date_____

- What is the pattern of the sequence? _____
- Is the sequence arithmetic or geometric? _____
- What is the next number in the sequence? _____
- What is an explicit formula for the sequence? _____

$A_{n+1} = A_n + 3$ and $A_1 = 5$

The diagram illustrates the recursive definition of the sequence. The formula $A_{n+1} = A_n + 3$ is shown at the top. Arrows point from this formula to the terms A_{n+1} , A_n , and A_1 . Below each term is a horizontal line, representing the sequence terms a_1, a_2, a_3, \dots respectively.

$$\begin{aligned} 5 \\ 8 &= 5 + 3 \\ 11 &= 8 + 3 \\ 14 &= 11 + 3 \\ 17 &= 14 + 3 \end{aligned}$$

What we call the 5th term? _____
 How do we find the 5th term if we know the 4th term? _____
 How do we write that? _____

How do we find the 6th term if we know the 5th term? _____
How do we write that? _____

How do we find the $(n+1)^{\text{th}}$ term if we know the n^{th} term? _____
How do we write that? _____

The statement $A_{n+1} = A_n + 3$ is a _____ formula. A recursive formula relates a _____ in the sequence to preceding _____ or _____ of the sequence.

NOTE: You may see the same sequence written as $A(n+1) = A(n) + 3$. It means the EXACT SAME THING!!!

Ex #2: Find the first five terms of the sequence defined by

$$A_{n+1} = A_n - 3 \text{ where } A_1 = 5$$

Ex #3: Find the first five terms of the sequence defined by

$$A_{n+1} = 3A_n \text{ where } A_1 = 5$$

Ex #4: Find the first five terms of the sequence defined by

$$f(n+1) = 2f(n) - 3 \text{ where } f(1) = 5$$

Ex #5: Find the first five terms of the sequence defined by

$$A_{n+1} = 3A_n + 4 \text{ where } A(1) = 1$$

Ex #6: Consider the sequence given by the formula

$$A_n = A_{n-1} - 5 \text{ where } A_1 = 12$$

The first five terms of the sequence are _____

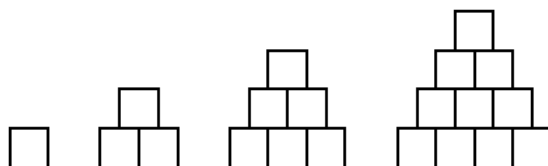
An explicit formula for the sequence would be _____

Find A_6 _____

Find A_{11} _____

Find A_{100} _____

Ex #6: A sequence of blocks is shown in the diagram below.



This sequence can be defined by the recursive function $a_1 = 1$ and $a_n = a_{n-1} + n$. Assuming the pattern continues, how many blocks will there be when $n = 7$?

- | | |
|-------|-------|
| 1) 13 | 3) 28 |
| 2) 21 | 4) 36 |

Ex #7: In 2014, the cost to mail a letter was 49¢ for up to one ounce. Every additional ounce cost 21¢. Which recursive function could be used to determine the cost of a 3-ounce letter, in cents?

- 1) $a_1 = 49$; $a_n = a_{n-1} + 21$
- 2) $a_1 = 0$; $a_n = 49a_{n-1} + 21$
- 3) $a_1 = 21$; $a_n = a_{n-1} + 49$
- 4) $a_1 = 0$; $a_n = 21a_{n-1} + 49$

Ex #8: Which recursively defined function represents the sequence 3, 7, 15, 31, ... ?

- 1) $f(1) = 3$, $f(n+1) = 2f(n) + 3$
- 2) $f(1) = 3$, $f(n+1) = 2f(n) - 1$
- 3) $f(1) = 3$, $f(n+1) = 2f(n) + 1$
- 4) $f(1) = 3$, $f(n+1) = 3f(n) - 2$